Real-Time Vision-Based Tracking Control of An Unmanned Vehicle

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Abstract

Recent advances in manufacturing automation have motivated vision-based control of autonomous vehicles operated in unattended factories, material handling processes, warehouse operations, and hazardous environment explorations. Existing vision-based tracking control systems of autonomous vehicles, however, have been limited in real-time applications due to slow and/or expensive visual feedback and complicated dynamics and control with nonholonomic constraints. This paper presents a practical real-time vision-based tracking control system of a three-wheeled unmanned vehicle, ViTra. Unlike the conventional RS170 video-based machine vision systems, ViTra uses a DSP-based flexible integrated vision system (FIVS) which is characterized by low cost, computational efficiency, control flexibility, and friendly user interface.

Especially, this paper focuses on developing a framework for vision tracking systems, designing generic fiducial patterns, and applying real-time vision systems to tracking control of autonomous vehicles. A laboratory prototype vision-based tracking system developed at Georgia Institute of Technology permits the uniquely designed fiducial landmarks to be evaluated experimentally, the control strategy and the path planning algorithm derived in the paper be validated in real-time, and the issues of simplifying nonlinear dynamics and dealing with nonholonomic constraints be addressed in practice. Experimental results reveal interesting insights to the design, manufacture, modeling, and control of vision-based tracking control systems of autonomous vehicles.

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1 Introduction

Advances in manufacturing automation have increased the demand for autonomous vehicles which can be operated in unattended factories, material handling processes, warehouse operations, and hazardous environment explorations. Automatic control of an unmanned vehicle requires real-time position and/or velocity feedback. One way to provide the feedback information is to use machine vision. However, commonly used RS170 video-based machine vision systems for the feedback have generally been computationally expensive and/or slow [1]. This paper investigates a practical machine vision system for locating and tracking, in real-time, a moving vehicle, and addresses the control issues of simplifying nonlinear dynamics and dealing with nonholonomic constraints of an unmanned vehicle.

The major difficulties encountered in vision-based tracking control are two-fold: slow and/or expensive visual feedback and complicated dynamics and control with nonholonomic constraints in "target-space" where the vehicle is located and oriented. Many attempts have been made in recent years to address the problem from the vision and/or the control perspectives. Due to the nonlinear dynamics and nonholonomic constraints inherent to the problem, controlling the vehicle in target-space has remained an unsolved research subject. In practice, however, the current strategy is to control the vehicle in "drive-space," where the vehicle is controlled, with an implementation of a path planning mechanism communicating between the target-space and drive-space. The feedback information in target-space is acquired by machine vision system, then passed through the path planning algorithm into the controller in drive-space. Therefore machine vision and motion path planning play critical roles on the overall system performance in this control scheme. Existing commercially available RS170 video-based machine vision systems for the feedback have been computationally expensive and/or slow, and so are not generally suitable for real-time, on-line applications. Potential improvement could be made on hardware innovation, embedded and efficient algorithm and software development, and generic fiducial landmarks design. In addition, the nonholonomic constraints which restrict the range of motion and degrade the maneuverability of the vehicle also need to be addressed in vehicle tracking control.
This paper focuses on developing a framework for vision tracking systems, designing
generic fiducial patterns, and applying real-time vision systems to tracking control of
autonomous vehicles. A control strategy is developed in drive-space to allow for a quick
and analytical design and implementation. A simple yet effective path planning mecha-
nism is devised to transform the information between the target-space and drive-space.
Nonholonomic constraint problem is also addressed in terms of vehicle design to enlarge
the range of motion and to improve the maneuverability of an autonomous vehicle. The
major contributions of this paper are: 1) the development of a practical method for
implementing real-time vision-based control of autonomous vehicles, 2) concept develop-
ment, design and experimentation of cost-effective generic fiducial landmarks, and 3)
derivation and experimental verification of compact motion planning algorithms which
effectively simplify nonlinear dynamics and controller design. The concepts, principles
and methods presented in the paper are applicable to vision-based control of a spectrum
of autonomous vehicles.

The rest of the paper is organized as follows. Section 2 presents the fundamentals
of vision tracking control with emphases placed on framework of vision tracking control
systems and fiducial pattern design. Section 3 develops the dynamic models and the
control strategy for a class of autonomous vehicles driven by DC servo motors. Section 4
describes a laboratory prototype vision tracking system including an innovative three-
wheeled autonomous vehicle, a real-time flexible integrated vision system (FIVS), and a
DSP-based experimental testbed with multimedia development environment. Section 5
details the system calibration and tracking experiments and summarizes the experimental
results. Finally, conclusions are drawn in Section 6.

2 Integrated Vision-based Control

2.1 Architecture of Vision-based Vehicle Control

Two commonly used configurations for vision-based vehicle control systems are space-
fixed and on-the-vehicle (on-board) vision systems. In the space-fixed configuration, a
stationary vision system is fixed in space and tracks a moving vehicle through a minimum
set of landmarks placed on the vehicle. The trade off, however, is that the range of motion
is restricted or more than one vision system is required. For a cost-effective solution to a large range of motion the vision system can be integrated on the vehicle. As a result, this on-the-vehicle configuration requires a set of landmarks or fiducial patterns as a medium, when analyzed by the vision system, to locate the vehicle. Figure 1 shows a conceptual schematic of a vision-based unmanned vehicle control system with the on-the-vehicle configuration. During operation, the vision system takes pictures of the fiducials periodically while the vehicle is moving, captures the patterns within its field of view, stores and analyzes the images, then returns the vehicle’s locations.

![Conceptual Schematic of a Vision-based Vehicle Control](image)

Figure 1: Conceptual Schematic of a Vision-based Vehicle Control

### 2.2 Fiducial Patterns

**Design Concept**

Fiducial patterns are used as landmarks to determine the vehicle’s location. A typical fiducial pattern usually consists of pattern members or primitives which are the basic elements or building blocks made-up the pattern and the configuration or arrangement of the members. Fiducial patterns can be effectively characterized using attributes in combination with structural information. The geometric features of a pattern member can, in general, be described in terms of its shape and size using a feature set $PE = \{\text{shape}, \text{size}\}$, where the elements themselves are geometric and numerical subsets, such as $\text{shape} = \{\text{square, circular, triangular, \ldots}\}$, and $\text{size} = \{\text{size}_1, \text{size}_2, \ldots, \text{size}_n\}$. 
Commonly used measures for the geometric variable, size, are the area or perimeter of the element. But it could also be the side for the square and radius for the circle, etc. [2]. The characteristics of a complete pattern can be represented by a pattern characteristic set $FP = \{PES, \text{spacing}, \text{orientation}\}$, where $PES = \{PE_1, PE_2, \ldots, PE_n\}$, $\text{spacing} = \{\text{spacing}_1, \text{spacing}_2, \ldots, \text{spacing}_{n_p}\}$, and $\text{orientation} = \{\text{orientation}_1, \text{orientation}_2, \ldots, \text{orientation}_{n_o}\}$. The fiducial pattern design, in particular, the geometric shapes and sizes of the pattern members and configuration of the members, is not unique and application-dependent. A good fiducial design, however, should 1) have simple and compact elements and structure, 2) require less computation for pattern recognition, and 3) provide reliable and accurate measurement information.

To eliminate background noise and thus to ensure the robustness of the fiducial patterns, it is preferable that the fiducials are made of retroreflective material. An ideal retroreflector returns light in the direction in which the light is incident. Retroreflective material appears bright and distinct in contrast to its background as seen by the photo-receptor. Detailed methods of achieving the effect of retroreflective fiducials can be found in [3]. The following example illustrates the method of giving retroreflective fiducial pattern a role in vision-based motion control.

**An Illustrative Example**

To illustrate the design concept, sample fiducial patterns are designed where two-size square pattern elements are employed, in other words, the feature sets are chosen as $\text{shape} = \{\text{square}\}$ and $\text{area} = \{\text{small, large}\}$, where the geometric dimension, size, is represented in terms of area. To construct a fiducial pattern, six members ($PES = \{PE_1, PE_2, \ldots, PE_6\}$) are arranged with five placed at the tips (vertices) and intersection point of a plus sign and one at the upper-left corner. Two distinct distances between two elements ($\text{spacing} = \{sp_1, sp_2\}$) are used to position the elements in a pattern. Two elements, the corner and center elements ($\text{orientation} = \{PE_{\text{corner}}, PE_{\text{center}}\}$), are designated to describe the pattern orientation. The following criteria illustrate the generic fiducial design.

a. The number of large blobs. Seven patterns with large blobs ranging from 0 - 6, as shown in Figure 2.
b. Spacing of the four cross blobs. Three characteristic resultant spacings between the four cross blobs are shown in Figure 3. The ratio of the sums of the blob spacings is \textit{small} : \textit{medium} : \textit{large}, where \textit{small} = 4sp_1, \textit{medium} = 2sp_1 + 2sp_2, and \textit{large} = 4sp_2.

Figure 3: Patterns with Three Distinct Characteristic Distances

c. Orientation of the corner blob relative to the center blob. Four possible combinations of the relative position and size of the corner and center blobs determine the orientation of the patterns (see Figure 4).

Figure 4: Combinations of Center and Corner Blobs

It is worth noting that the number of patterns for the illustrative example is $2 \times 3 \times 1 + 2 \times 3 \times 3 + 3 \times 3 \times 4 = 60$. An implementation example of the designed fiducials is shown in Figure 5. A typical image of the fiducial patterns is given in Figure 6. Notice that the intended background noises, the white strips, on the fiducial board in Figure 5
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do not appear in the fiducial image. That is due to the use of retroreflective material for the fiducial patterns.

Figure 5: Fiducial Patterns

Figure 6: A Typical Image of the Fiducial Patterns

2.3 Pattern Recognition Algorithm

The fiducial patterns are recognized through a pattern recognition algorithm of template matching [4][5]. A template matching pattern recognition algorithm for vision tracking control usually performs two major functions: (1) identifies primitives, composes image patterns, and matches the constructed image patterns with fiducial patterns; (2) computes measurement (e.g., position and orientation) information and transforms the
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information from image coordinate to world coordinate. A basic template matching pattern recognition system consists of two basic modules, segmentation or decomposition and “triangulation” or composition involving pattern primitives (including relations among primitives and subpatterns), and structural analysis. The segmentation module uses algorithms, for example a region-growing algorithm [6], to find all the primitives or elements within the field of view of the CCD camera. It also computes the numerical attributes, such as the center of gravity, \((t_x, t_y)\) and the area of the primitives found. The triangulation module then constructs image patterns by finding relations among primitives or subpatterns. As an example, the six blobs closest to the center of gravity are used to compose an image pattern for the illustrative fiducial design described in Section 2.2. The triangulation module uses the information from segmentation to uniquely match the image with one of the patterns stored in the fiducial pattern database. The patterns in the database are used to determine the vehicle position since each pattern has a known, fixed position associated with it. Since the image is not always aligned with the fiducial patterns, the triangulation module also uses a matrix algorithm to convert the vehicle position from the image coordinate to a real world coordinate through the transformation

\[
Q_{\text{world}} = \text{world } T_{\text{image}} Q_{\text{image}}
\]  

(1)

where \(Q_{\text{world}}\) and \(Q_{\text{image}}\) are the vehicle positions in world coordinate and image coordinate, respectively; and \(\text{world } T_{\text{image}}\) is the transformation between the two coordinates. For the example given in Figure 1 the transformation is given by the following matrix equation:

\[
\begin{bmatrix}
  x_{\text{center}} & x_{\text{corner}} \\
  y_{\text{center}} & y_{\text{corner}}
\end{bmatrix}_{\text{world}} = \begin{bmatrix}
  \cos \theta_i & -\sin \theta_i & t_x \\
  -\sin \theta_i & -\cos \theta_i & t_y
\end{bmatrix} \begin{bmatrix}
  x_{\text{center}} & x_{\text{corner}} \\
  y_{\text{center}} & y_{\text{corner}} \\
  1 & 1
\end{bmatrix}_{\text{image}}
\]

where \(t_x, t_y, \) and \(\theta_i\) are translation and rotation displacements of the pattern image relative to the corresponding fiducial pattern. On matching an image with one of the patterns, the triangulation module returns the \((x, y, \theta)\) position and orientation of the vehicle. This information is used by a control algorithm to determine appropriate control action. A flowchart of the recognition algorithm is given in Figure 7.
3 Dynamic Modeling and Control Strategy

In this section, we present dynamic modeling, path planning, and control strategy development for three-wheeled autonomous vehicles. First, we obtain the complete set of dynamic models including vehicle dynamics and motor characteristics. We then propose a path planning mechanism, a transformation from the target-space to the drive-space, to simplify the nonlinear dynamics and the controller design. Finally, we outline the control strategy development in the drive-space.

3.1 Dynamic Modeling and Path Planning

A comprehensive motion description of a vehicle should be a dynamic model in terms of the motor armature voltages as inputs and the vehicle position and orientation as outputs. However, the dynamic modeling of the vehicle can be decomposed into vehicle dynamics and motor characteristics for simplicity.

Vehicle Dynamics

The following two assumptions are made in deriving the vehicle dynamics. 1) The vehicle is modeled as a rectangular plate of dimensions $l \times b \times h$ with uniform mass distribution. 2) The axes of the driving motor shafts are perfectly aligned and are located directly below the transversal axis of the vehicle. Using the Lagrangian formulation,
equations of motion for the vehicle are obtained in terms of position $x, y$ of the center of gravity of the vehicle and orientation $\theta$ of the axis of the drive shafts; the results are given in Equations (2) \sim (4)

\begin{align*}
(3m + M)\ddot{x} - \frac{1}{2} M\dot{x}\dot{\theta}\sin 2\theta + (3m + M \cos^2 \theta)\dot{\theta}\dot{y} &= \frac{\tau_l + \tau_r}{R} \sin \theta, \\
-(3m + M)\ddot{y} + (3m + M \sin^2 \theta)\dot{\theta}\dot{x} - M\dot{\theta}\ddot{x} - \frac{1}{2} M\dot{\theta}\dot{y}\sin 2\theta &= \frac{\tau_l + \tau_r}{R} \cos \theta, \\
(0.75m l^2 + \frac{1}{12} M(b^2 + l^2))\ddot{\theta} &= \frac{\tau_l - \tau_r}{2R} l,
\end{align*}

where $\tau_l$ and $\tau_r$ are the torques applied at the left and right wheels respectively, $R$ is the radius of the rear wheels, and $M$ and $m$ represent the masses of the wheel and the body of the vehicle respectively.

**Motor Characteristics**

The motor characteristics referred to here are the dynamic models which relate angular displacement of each wheel to the respective armature control voltage. A typical transfer function for an armature controlled DC motor is given by Equation (5), with armature voltage as the input and shaft angular displacement as the output.

\[ G(s) = \frac{\theta_m(s)}{V(s)} = \frac{K}{s(\tau s + 1)}, \]

where $K$ and $\tau$ are the gain and time-constant, respectively.

**Path Planning**

Notice that the vehicle dynamics, described by Equations (2) \sim (4), are highly non-linear and coupled. Even the linearized version of the dynamics is time-varying due to the large range of motion. It is, therefore, preferable that the controller is designed in drive-space based on the motor characteristics. The implementation of this simplified controller design, however, requires transformations relating the drive-space to the target-space parameters in path planning.

With the aid of Figure 8, the transformation from the location and orientation of the CCD camera to that of the driving wheels of the vehicle are established by the following kinematic approximations.
\[ x_l = x + p \sin \theta - q \cos \theta, \quad y_l = y - p \cos \theta - q \sin \theta, \quad (6) \]
\[ x_r = x + p \sin \theta + q \cos \theta, \quad y_r = y - p \cos \theta + q \sin \theta, \quad (7) \]

where \( x_l, y_l, \) and \( x_r, y_r, \) represent the \( x \) and \( y \) locations of left and right wheels respectively. Figure 8 also shows a generic path of the vehicle. Note that a small distance travelled by the vehicle along a curve can be approximated by a straight line. Hence, we have:

\[ \theta_{ml} = \frac{1}{R} \left[ (x_l^d - x_l^c)^2 + (y_l^d - y_l^c)^2 \right]^{\frac{1}{2}}, \quad (8) \]
\[ \theta_{mr} = \frac{1}{R} \left[ (x_r^d - x_r^c)^2 + (y_r^d - y_r^c)^2 \right]^{\frac{1}{2}}, \quad (9) \]

where \( \theta_{ml} \) and \( \theta_{mr} \) are the approximate left and right wheel angular displacements; and the superscripts "c" and "d" represent the current and desired locations of the vehicle. Using Equations (6) \(~ (7)\) in Equations (8) \(~ (9)\), the target-space parameters, position and orientation of the vehicle \((x, y, \theta)\), can be converted to the drive-space parameters, motor shaft angular displacements \((\theta_{ml}, \theta_{mr})\).

### 3.2 Control Strategy Development

The control objective here is to maneuver a vehicle to follow a prescribed path / trajectory utilizing the visual feedback and modern digital control techniques. As control functions will be implemented using DSP and/or computers, we design the controllers
in the discrete-time domain. First, we give a discretized state-space representation of the motor dynamics. The pole placement technique is then used to design the regulator in order to obtain specified time response of the system. In the case where the vision system is used to measure only the vehicle's position, a reduced-order observer can be designed to estimate the vehicle's velocity necessary for full state feedback. Finally, a digital tracking filter is designed to generate the reference input for following a desired trajectory.

The discretized state-space model of the motor dynamics, Equation (5), with the zero-order hold is given by

\[ X(k+1) = AX(k) + Bu(k), \]  
\[ y(k) = CX(k), \]  

where

\[ X(k) = \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}, \quad A = \begin{bmatrix} 1 & A_{12} \\ 0 & A_{22} \end{bmatrix}, \quad B = \begin{bmatrix} B_1 \\ B_2 \end{bmatrix}, \quad C = \begin{bmatrix} 1 & 0 \end{bmatrix}, \]

and where \( A_{12} \overset{\Delta}{=} \tau(1-e^{-\frac{T}{\tau}}), \ A_{22} \overset{\Delta}{=} e^{-\frac{T}{\tau}}, \ B_1 \overset{\Delta}{=} K(T+A_{12}), \) and \( B_2 \overset{\Delta}{=} K(1-A_{22}). \) \( T \) is the sampling period. Note that in Equations (10) ~ (11), \( x_1(k) \) and \( x_2(k) \) denote the angular displacement and angular velocity of the motor shaft respectively, \( u(k) \) represents the voltage input to the motor armature, and \( y(k) \) is the angular position output, all at the \( k^{th} \) sampling instant. Based on the state-space representation and the separation principle, the regulator and the observer for the discretized system are designed independently in the following.

**Regulator and Reduced-order Observer Design**

The time response specifications for the regulator design are denoted as: settling time = \( t_s \) sec and maximum percent overshoot \( \leq M_p. \) These specifications of time response characteristics correspond to the desired pole locations \( \sigma_d \pm j\omega_d \) for the closed-loop system. Since the full state feedback control law is \( u(k) = -K_r x(k), \) where \( K_r \) is the regulator gain matrix, the closed-loop system dynamics are then given by \( x(k+1) = Ax(k), \) where \( A = A - BK_r. \) The regulator gain, \( K_r, \) can be determined by placing
the poles of \( \hat{A} \) at the desired locations. In the case where a reduced-order observer is designed to estimate the angular velocity \( x_2(k) \), the observer gain, \( L_r \), can be determined by placing the poles of \( \hat{A}_e = A_{22} - L_r A_{12} \) at a desired location, \( \sigma_o \).

**Digital Tracking Filter Design**

In the previous subsection, we outlined the design procedure for the digital state feedback regulator and reduced-order observer to achieve specified time response characteristics. Furthermore, in order to follow an arbitrary desired time-varying trajectory, we need to implement a digital tracking filter in the feedforward loop. The tracking filter design for the vehicle control system is based on the resultant closed-loop transfer function

\[
G_{cl}(z) = \frac{K_{cl}(z + z_0)}{(z - \sigma_d - j\omega_d)(z - \sigma_d + j\omega_d)}
\]

where \( K_{cl} \) is the closed-loop gain constant and \( -z_0 \) is a closed-loop zero. Notice that when the closed-loop zero, \( z = -z_0 \), is near the point \((-1 + j0)\) in the complex plane it is not advisable to perform direct zero-pole cancellation, or in other words, to use \( G_{cl}^{-1}(z) \) as the feedforward digital tracking filter. Otherwise, the closed-loop zero, \( z = -z_0 \), becomes a pole of \( G_{cl}^{-1}(z) \) which will generate an oscillatory reference signal. In this case, a zero phase error tracking filter (ZPETF) [7] can be designed. The following ZPETF generates the reference input for the closed-loop system consisting of the state feedback regulator and the reduced-order observer.

\[
r(k) = K_t[a_{-1}y_d(k - 1) + a_0y_d(k) + a_1y_d(k + 1) + a_2y_d(k + 2)],
\]

where \( r(k) \) denotes the reference input to the closed-loop system at the sampling instant \( k \); \( a_i(i = -1, 0, 1, 2) \) is a constant coefficient to be determined based upon the motor parameters, controller design specifications, and sampling period; \( y_d(\cdot) \) represents the desired wheel angular displacement at the sampling instant \( (\cdot) \); and \( K_t \) is the tracking filter gain which is determined experimentally.

## 4 Laboratory Prototype

To demonstrate the principle and concept of vision tracking control of an unmanned vehicle, a prototype system has been designed and constructed. The laboratory prototype
system consists of three basic subassemblies, a three-wheeled autonomous vehicle, ViTra, a real-time flexible integrated vision system (FIVS), and a DSP-based experimental testbed with a multimedia development environment.

4.1 Three-wheeled Autonomous Vehicle

Maneuverability of a vehicle is essential to determine tracking performance of the vehicle since the effectiveness of control action depends on the vehicle's dynamics. For a quick and smooth dynamic response, the vehicle should have a smooth driving and transmission mechanism, must be able to turn freely in all directions, and contain minimum inertia yet enough weight to provide necessary contact force on the ground to prevent from slipping.

To meet the vehicle design criteria, a three-wheel configuration with two rear driving wheels and a ball-joint-like universal front wheel is chosen for the autonomous vehicle, ViTra. The two rear driving wheels are geared to two DC motors controlled by power amplifiers. Use of two, instead of three or four, driving wheels simplifies the drive mechanism and the control of the vehicle, reduces the backlash, friction and stiction of the transmission system, and lowers the system inertia. The ball-joint-like front wheel allows the vehicle to maneuver in all directions without slip. Also, the universal front wheel eliminates its nonholonomic constraints inherent in conventional wheeled vehicles. The prototype design of the vehicle is shown in Figure 9.

4.2 Flexible Integrated Vision System (FIVS)

To form a feedback control loop and to enhance real-time path planning and trajectory tracking, the vehicle’s position needs to be measured, then compared with the reference or desired position, and the resulting error fed back to the controller for appropriate control action. The ViTra solution to providing the feedback information is the FIVS [8], developed at Georgia Institute of Technology.

The FIVS, as its name refers, is a stand-alone machine vision system which integrates imaging sensors, control, illumination, signal processing, and data communication in a single unit. A prototype system is shown in Figure 10. The FIVS has five basic functional modules: 1) an on-board DSP 56001 digital signal processor made by Motorola and the associated EEPROM, scratch RAM, and communication hardware, 2) a video head
including an image sensor (TC-211 CCD by Texas Instruments), a high-bandwidth signal conditioning amplifier, a flash A/D converter, and a video RAM (VRAM), 3) an optic system with lens and illumination, 4) an off-line host-interface for system calibration, image analysis, and application-dependent software implementation, and 5) a real-time video record/playback for failure-mode detection.

An application development environment accompanying the hardware is developed to: 1) provide users with the flexibility to control the CCD array scanning, integration time, and illumination intensity; 2) allow image processing to be done on-board in real-time using the DSP; and 3) permit the process controller to setup and calibrate the
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vision system, and to analyze any possible failure modes. Integrating the hardware and software, the FIVS is characterized by low cost, computational efficiency, flexibility, and friendly user interface.

4.3 Experimental Testbed

The ViTra control system integrates the three-wheeled autonomous vehicle, an on-board FIVS, a ceiling fiducial board, a digital signal processor (DSP) board with A/D and D/A converters, and an Intel 486 as central computer. As shown in Figure 9, the FIVS is mounted at a constant offset rear position from the center of mass of the vehicle in order to balance the weight of the vehicle and provide the necessary contact on the ground to avoid slip of the rear driving wheels. The central computer communicates with the FIVS via an RS-232 serial port. Power amplifiers connect the DSP and the driving motors through a power cable. All the major components are properly connected and integrated through a feedback control scheme. The central computer receives measured kinematic information of the vehicle from the FIVS, then compares it with a reference obtained from the path planning mechanism. The difference is fed back to the controller for appropriate control action. The controller output voltage signals sent to the power amplifiers direct the vehicle to the desired location. This feedback scheme continues until the vehicle reaches then follows the desired reference signal.

The main objective of the experiment is to integrate the FIVS, DSP, and central computer to perform real-time digital tracking control of the unmanned vehicle. The FIVS, as a noncontact sensor, must provide quick and reliable real-time feedback information (position and/or velocity measurements) for closed-loop control. The DSP, which is implemented to perform the inner loop (low-level) control functions, needs to have a faster update rate than the outer feedback loop. The computer, as a central communication and decision-making unit, must be able to coordinate the FIVS, DSP, and vehicle, plan the path/trajectory on-line, and generate control reference signals for accurate trajectory following.

To achieve fast, real-time control of the vehicle, a DSP board, dSPACE DS1102, is used to perform the inner loop control function. MATLAB/SIMULINK with Real-Time Workshop is used to generate the C code for DSP implementation. The dSPACE DS1102
interface with MATLAB allows SIMULINK to communicate with the on-board A/D and D/A converters; it also allows the C-code generated by the workshop to be downloaded directly to the DSP board to perform real-time function.

To ensure accurate trajectory tracking, the outer position feedback loop is formed based on the FIVS measurement. As discussed in Section 4.2, the FIVS by itself is an independent unit with an on-board DSP. All the functions of taking fiducial pictures, storing and analyzing images, and returning position and orientation information, are performed on-board in real-time. On each outer loop control cycle, the FIVS takes one fiducial picture, stores and processes the image, then returns the position information. A ceiling fiducial board with the fiducial patterns uniquely designed in Section 2.2 is placed on a ceiling as the landmarks of the FIVS measurement system. Since the field of motion is restricted to 5' x 6' for the experiment, only 30 patterns were used for simplicity and computational efficiency. All the 30 patterns are properly spaced on the ceiling board of 5' x 6', so that at least one complete pattern will be captured by the FIVS at each exposure. The experimental implementation of the designed fiducials is shown in Figure 5.

An Intel 486 (66Hz) is used to coordinate the DSP and the FIVS, and to execute the functions such as path planning and reference signal generation for trajectory tracking. The central computer communicates with the DSP board using the DSP shared memory; and talks to the FIVS through a serial port. On every outer loop control cycle, the central computer commands the FIVS to take a picture of the fiducials; the FIVS processes the image, then returns the current position of the CCD camera; the central computer stores the data in the DSP shared memory. Whenever the DSP control loop cycle starts, the DSP reads the shared memory as the inner control loop reference. It is worth noting that the inner control loop frequency is much faster than that of the outer control loop (at a sampling ratio 0.001:0.1 for the experiment). The fast inner control loop frequency is advantageous to the stability and the dynamic response of the system. The path is planned based on the measurement of the position and orientation of the vehicle and the coordinate transformation from the target-space to the drive-space, as discussed in Section 3.1. It is worth emphasizing that this experimental testbed aims at demonstrating the concepts of integrated vision-based motion control. Once the concepts are proven,
modifications of the existing prototype to eliminate the communication and power cables using wireless communication or radio-controlled devices and on-board battery power supply are relatively straightforward.

5 Experimental Investigation

Experiments are performed to calibrate the FIVS, to test the fiducial patterns, and to control the vehicle to track a specified circular path/trajectory.

5.1 Experimental Parameters

The characteristics of the motors used to drive ViTra have been determined experimentally, and the results are summarized as: the gain $K = 103.85 \text{ rad/}sec \cdot V$ and the time constant $\tau = 0.05 \text{ sec}$. Based on the motor characteristics, a regulator is designed to achieve desired time response specified by settling time $t_s = 0.1 \text{ sec}$ and maximum percent overshoot $M_p \leq 5$. These specifications correspond to the desired closed-loop locations $0.9717 \pm j0.0275$. The regulator gain which places the closed-loop pole at the desired locations are determined to be $K_r = [0.3979 \quad 0.0095]$. A reduced-order observer is designed in the experiment to estimate the vehicle’s velocity. The observer gain, $L_r$, is determined by placing the poles of the estimation error system at the desired position, $\sigma_o = 0.5$, and the result is found to be $L_r = 486.7650$. Implementation of the regulator and observer yields the following closed-loop z-transfer function

$$G_{cl}(z) = \frac{0.002(z + 0.9937)}{(z - 0.9717 - j0.0275)(z - 0.9717 + j0.0275)}.$$

A zero phase error tracking filter with unit gain is then designed to be

$$r(k) = 1.0063y_d(k - 1) + 3.0695y_d(k) + 0.9916y_d(k + 1) - 1.0582y_d(k + 2).$$

5.2 Implementation Issues

Several implementation issues of importance to the overall system performance are discussed in the following.

Hybrid Use of Position Measurement and Prediction
In theory, the position measurement should be fully used to estimate the velocity and to form the inner feedback loop. In practice, however, due to the limited FIVS speed and measurement error, the position measurement is weighted by a scaling factor less than one; it is then used together with a weighted predicted position from the motor dynamics. The experimentally determined motor dynamics is shown to be fairly accurate to use. The hybrid position feedback and the velocity observation improve the reliability and the performance of the system. The “optimum” weights with respect to the measured and predicted position determined by experimentation are 0.2 and 0.8 respectively for the circular path tracking.

**Motor and Amplifier Calibration**

Calibration plays an important role in determining the accuracy of a system. Calibrations of the ViTra control system include the calibration of the amplifiers and the FIVS. Although the two driving motors are assumed to be identical in the dynamic modeling, experiments showed a slight difference between the characteristics (the parameters of the models) of the motors. For example, applying an equal voltage to both motors does not result in a straight line motion of the vehicle. One way to calibrate the motors is to cascade a small variable resistor in one of the motor armatures. The characteristics of the two motors are balanced by adjusting the variable resistance. Although this approach introduces additional electrical power consumption into the system, the cascaded resistor can be used to measure the velocity and then to form a measured velocity feedback to overcome the possible motor stall problem as will be discussed in the following.

**Initial Starting Current and Motor Stall Problem**

Due to stiction, inertia, and vehicle load, the motors require higher voltage inputs to start than they require in the steady state (normal operating condition). To overcome the friction during start-up etc., the controller is designed such that the closed-loop system has an overshoot of about 5%. An alternative is to implement measured velocity feedback using the cascaded resistor in the motor armature. During motor start-up or motor stall, the controller senses the near zero velocity, then takes proper control actions. The first approach, however, is used in this experiment for simplicity.
5.3 FIVS Static Tests and Calibration

For the experiment, the location of the ceiling fiducial board on which the patterns are placed is approximately 9.75 ft above the CCD lens (focal point) or $H = 9.75ft$ as shown in Figure 1. The CCD is a fixed known distance behind the lens. This information is used to compute the scale factor between the actual and computed images in calibration.

A calibration module, which operates on "pcx" files and performs all the functions of segmentation and triangulation, is developed to calibrate the FIVS measurement system. Sample experiments were carried out for different vehicle positions and orientations around a predetermined trajectory. The characteristic trajectory was selected to be a circle of 20 inch radius centered at the geometric center of the ceiling board projection on the ground. Tables 1 and 2 list the known and measured vehicle positions. Figures 11 ~ 13 give the corresponding plots.

<table>
<thead>
<tr>
<th>Table 1: Known and Measured Position Data</th>
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<tbody>
<tr>
<td>Known Positions</td>
</tr>
<tr>
<td>x</td>
</tr>
<tr>
<td>---</td>
</tr>
<tr>
<td>1</td>
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From Figure 13, we observe that the measured orientations of the vehicle accurately match the known, world orientations. The average deviation from the known orientation is about 1.16 degrees which is small considering the difficulty encountered in aligning the vehicle with the known coordinate system. The accuracy defined as the ratio of average deviation to workspace is about 0.32%. The measured $(x, y)$ position data, as shown in Figures 11 and 12, are slightly off from the known positions. The average position deviation from the true position is about 2.92 and 2.63 inches with the accuracies of 4.86%
Table 2: Known and Measured Orientation Data

<table>
<thead>
<tr>
<th>Known Orientations</th>
<th>Measured Orientations</th>
</tr>
</thead>
<tbody>
<tr>
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<td>8</td>
<td>330.00</td>
</tr>
<tr>
<td>9</td>
<td>360.00</td>
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</tbody>
</table>

Figure 11: Known vs Measured Vehicle $x$-positions

and 3.65% for the $(x, y)$ coordinates respectively. The discrepancy between the known and the measured positions is due to the level of the CCD lens and the lighting conditions etc. The CCD lens must be perfectly leveled (pointing vertically to the ceiling pattern board) to ensure precise measurement. Overall, the pattern recognition algorithm and the fiducial patterns worked fairly well for the experiment.

5.4 Trajectory Tracking Results and Discussions

The control algorithms designed in Sections 3.2 and 5.1 are implemented through host and DSP programs to track a desired circular path with radius of 20 inches. A number of trajectory tests are performed, and two typical paths are recorded and plotted in Figure 14.
As shown in Figure 14, the overall real paths approximately follow the desired ones. Examination of paths 1 and 2 in Figure 14 shows a reasonably good repeatability of the tests. There are, however, some data points on the real paths relatively far from the desired paths. This is mainly due to the mismatch of the FIVS update rate and the vehicle’s moving speed. The discrepancy can be reduced by optimizing the pattern recognition algorithm, hence increasing the FIVS update rate, and by introducing measured velocity feedback into the control loop. The following factors may have also contributed to the trajectory discrepancy: 1) unmodeled friction, 2) not perfectly leveled ceiling board, and 3) approximation in path planning. It is expected that the discrepancy can
be further minimized by improved modeling and more sophisticated system calibration and controller design.

6 Conclusions

A practical vision-based tracking control system for an unmanned vehicle, ViTra, has been presented in this paper. Unlike conventional machine vision systems, ViTra uses a DSP-based flexible integrated vision system (FIVS) which is characterized by low cost, computational efficiency, flexibility, and friendly user interface. The uniquely designed fiducial patterns and corresponding pattern recognition algorithm better facilitated the FIVS machine vision system. The innovative design of ViTra improved the maneuverability of the vehicle, and eliminated the nonholonomic constraints of the front wheel inherent in traditional wheeled vehicles. The DSP implementation of the digital controllers and observer designed in the paper showed the practicability of using modern control techniques to enhance the system performance. Practical control issues such as simplifying nonlinear dynamics and dealing with nonholonomic constraints have also been addressed in the paper.

A number of static tests demonstrated the FIVS’s precision measurement of the vehicle’s position and allowed accurate calibration of the FIVS. Sample circular trajectory
tracking experiments illustrated the possibility of using FIVS in real-time tracking applications of unmanned vehicles. Research work is currently being directed toward optimizing the fiducial patterns and pattern recognition algorithm, further improving the maneuverability of the vehicle, and conducting various trajectory tracking tests.

Acknowledgement

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References


